CPSC 340: Machine Learning and Data Mining

Convolutional Neural Networks (and miscellaneous deep learning tricks) Spring 2022 (2021W2)

Admin

• A6 is out. Get it done early!

– Due April 8th

- Bonus! 100% grade in class for anyone who attends today's class virtually!
 - Click here to redeem offer within 2 minutes:
 - <u>https://tinyurl.com/100percentGradeFor340</u>

Admin

• Plan for April 6th (next wed)

– An experiment!

- We will watch two videos from my research past
 With live questions!
- Deep Visualization Toolbox:

https://www.youtube.com/watch?v=AgkflQ4IGaM

- Deep Learning Overview & Visualizing What Deep Neural Networks Learn
- https://www.youtube.com/watch?v=3lp9eN5JE2A

But first

• A want to briefly revisit two things I flew through

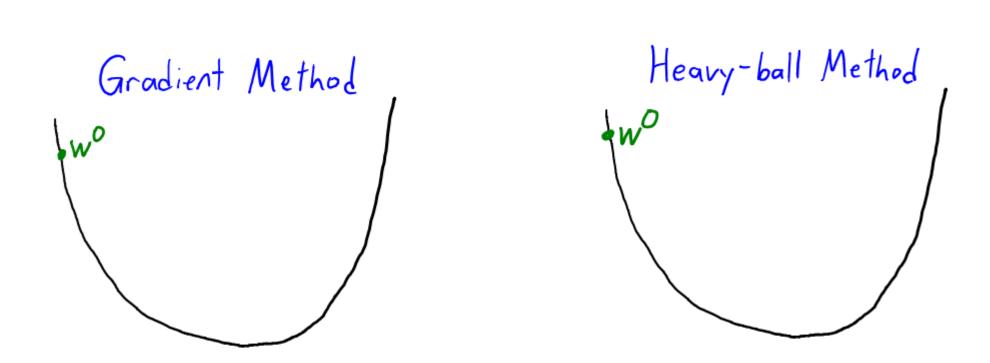
Setting the Step-Size

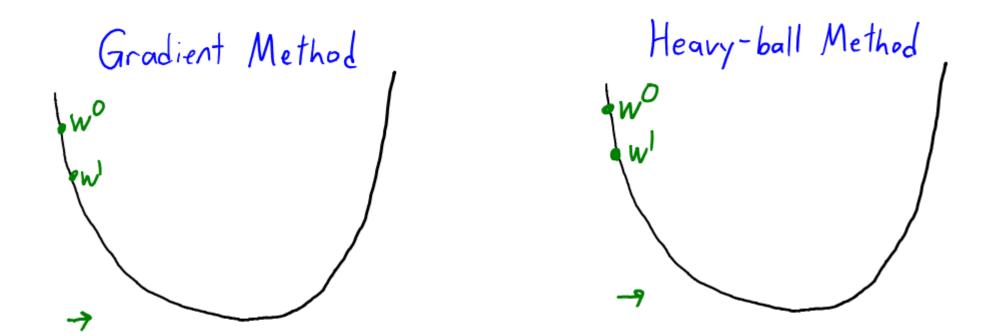
- Stochastic gradient is very sensitive to the step size in deep models.
- Bias step-size multiplier: use bigger step-size for the bias variables.
- Momentum (stochastic version of "heavy-ball" algorithm):
 - Add term that moves in previous direction:

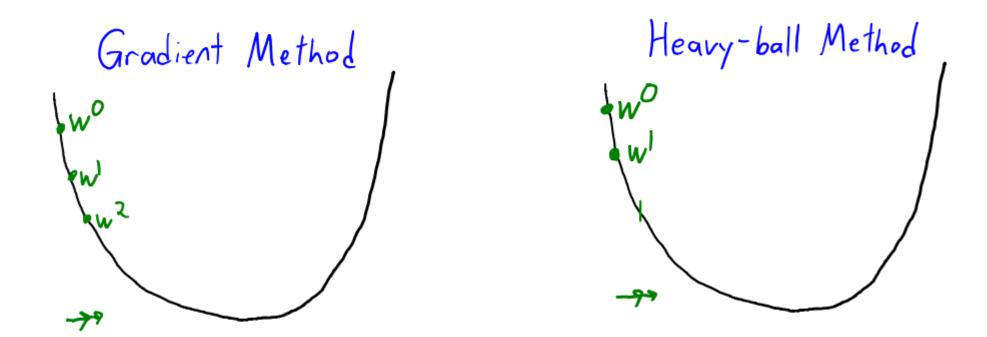
$$W^{t+1} = W^{t} - \alpha^{t} \nabla f_{i} (w^{t}) + \beta^{t} (w^{t} - w^{t-1})$$

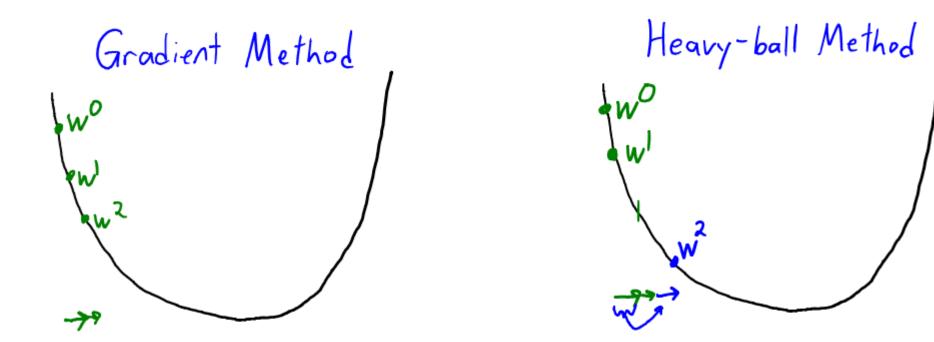
skeep going in the old direction

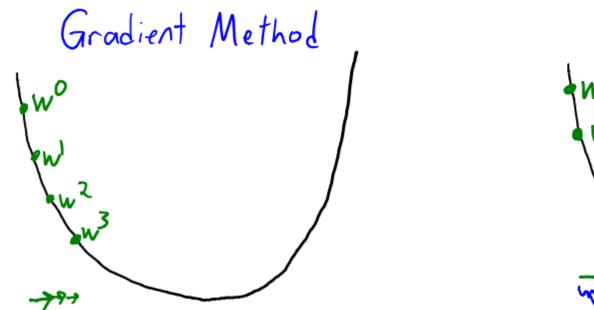
– Usually $\beta^{t} = 0.9$.

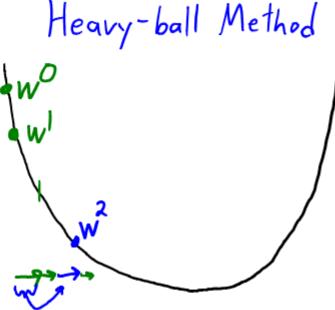


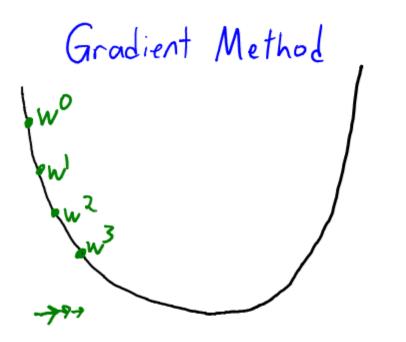


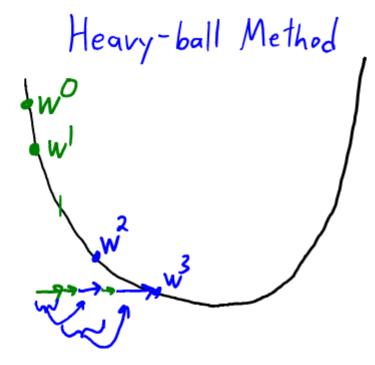


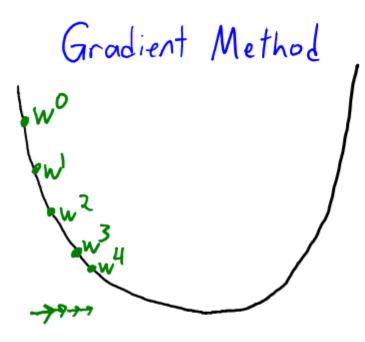


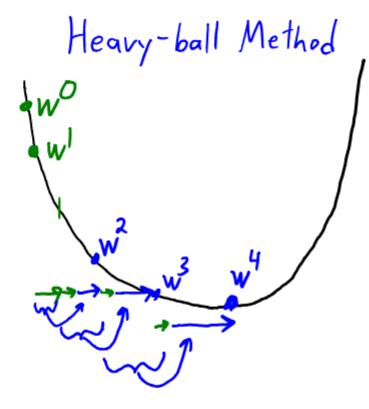


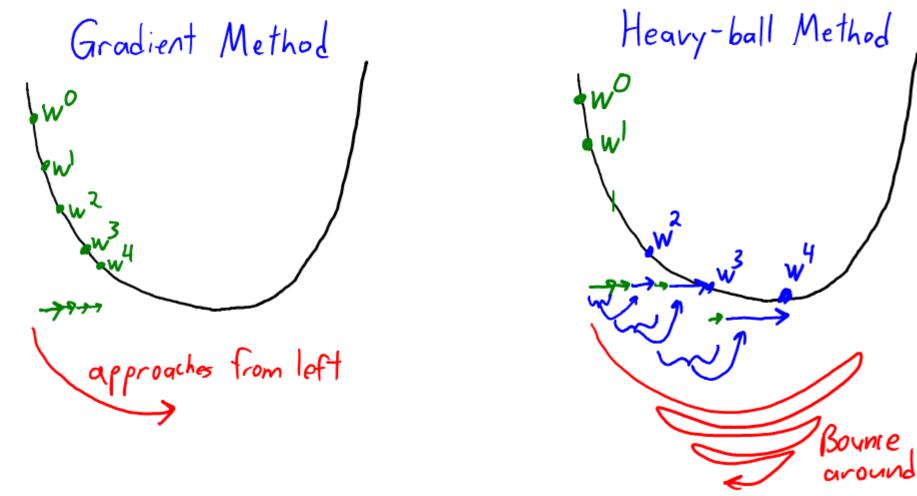










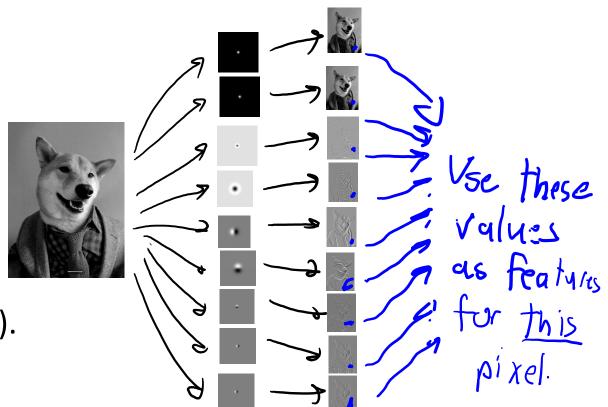


Good demo to check out: https://distill.pub/2017/momentum/

Convolutions as Features

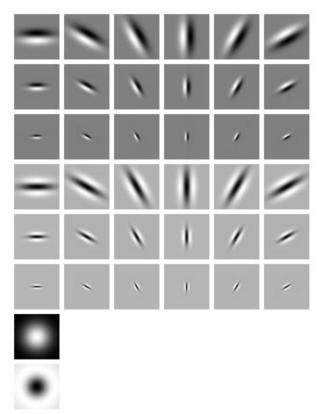
- Classic vision methods use convolutions as features:
 - Usually have different types/variances/orientations.
 - Can take maxes across locations/orientations/scales.
- Notable convolutions:
 - Gaussian (blurring/averaging).
 - Laplace of Gaussian (second-derivative).
 - Gabor filters

(directional first- or higher-derivative).



Filter Banks

- To characterize context, we used to use filter banks like "MR8":
 - 1 Gaussian filter, 1 Laplacian of Gaussian filter.
 - 6 max(abs(Gabor)) filters:
 - 3 scales of sine/cosine (maxed over 6 orientations).



• Convolutional neural networks (next time!) are replacing filter banks.

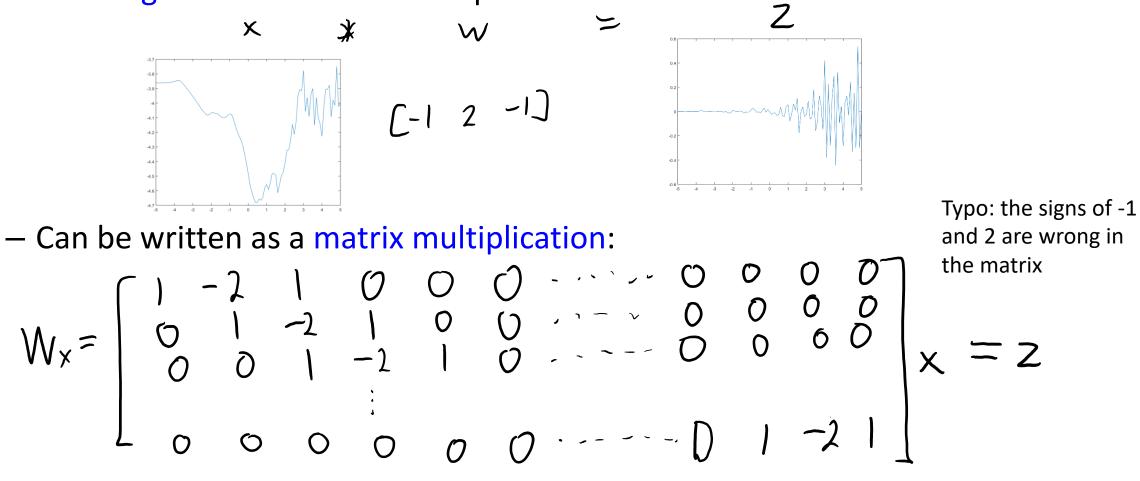
http://www.robots.ox.ac.uk/~vgg/research/texclass/filters.html

Now back to our regularly scheduled program

1D Convolution as Matrix Multiplication

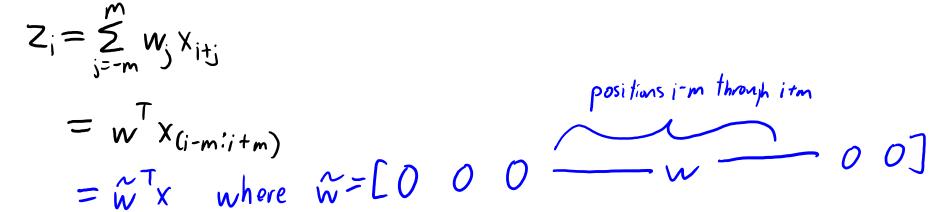
• 1D convolution:

- Takes signal 'x' and filter 'w' to produces vector 'z':



1D Convolution as Matrix Multiplication

• Each element of a convolution is an inner product:



• So convolution is a matrix multiplication (I'm ignoring boundaries):

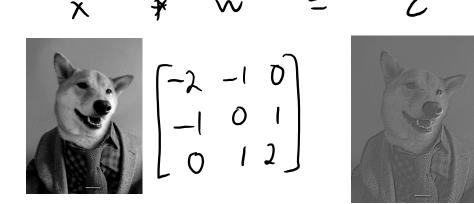
$$z = \widetilde{W}x$$
 where $\widetilde{W} = \begin{bmatrix} 0 & w & 0 & 00 \\ 0 & 0 & w & 0 \end{bmatrix}$
 $\begin{bmatrix} matrix & can & be \\ 0 & 0 & 0 & w \\ 0 & 0 & 0 & w \end{bmatrix}$
The charter (w) is the more sparse the matrix is only has $2m+1$ variables.

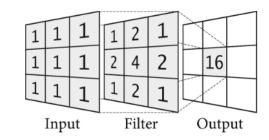
The shorter 'w' is, the more sparse the matrix is.

2D Convolution as Matrix Multiplication

• 2D convolution:

- Signal 'x', filter 'w', and output 'z' are now all images/matrices:



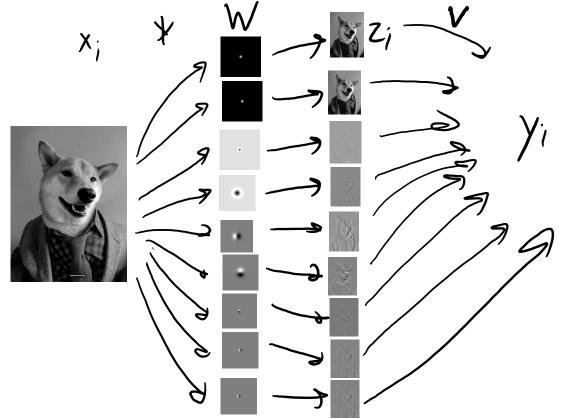


- Consider training neural networks on 256 by 256 images.
 This is 256 by 256 by 3 ≈ 200,000 inputs.
- If first layer has k=10,000, then it has about 2 billion parameters.
 - We want to avoid this huge number (due to storage and overfitting).
- Key idea: make Wx_i act like several convolutions (to make it sparse):

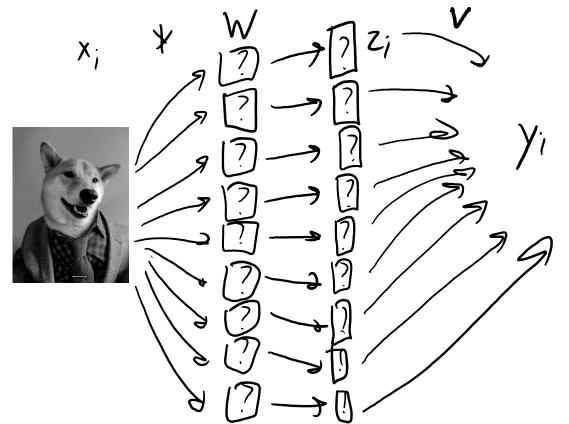
- 1. Each row of W only applies to part of x_i .
- 2. Use the same parameters between rows.

• Forces most weights to be zero, reduces number of parameters.

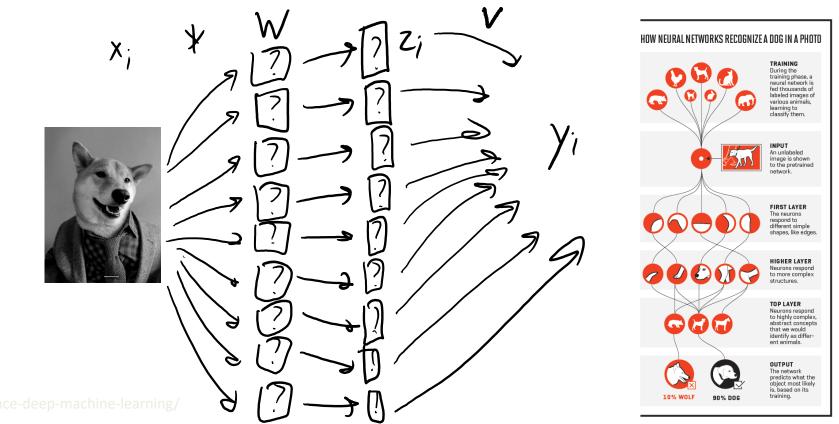
- Classic vision methods uses fixed convolutions as features:
 - Usually have different types/variances/orientations.
 - Can do subsampling or take maxes across locations/orientations/scales.



- Convolutional neural networks learn the convolutions:
 - Learning 'W' and 'v' automatically chooses types/variances/orientations.
 - Don't pick from fixed convolutions, but learn the elements of the filters.

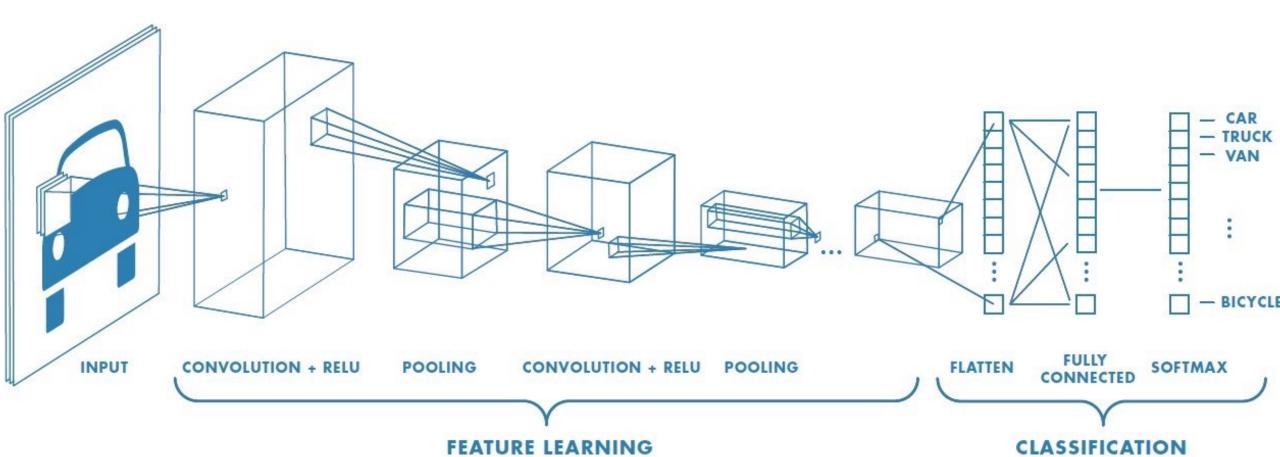


- Convolutional neural networks learn the convolutions:
 - Learning 'W' and 'v' automatically chooses types/variances/orientations.
 - Can do multiple layers of convolution to get deep hierarchical features.

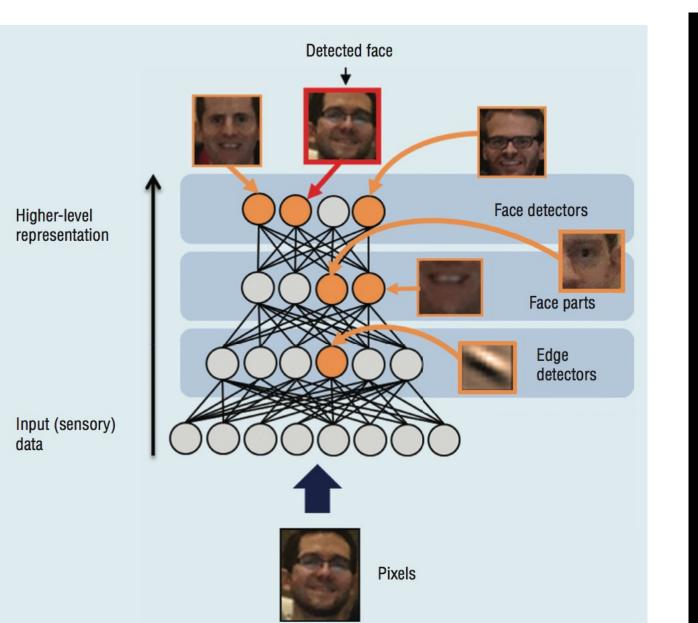


Two Main Motivations

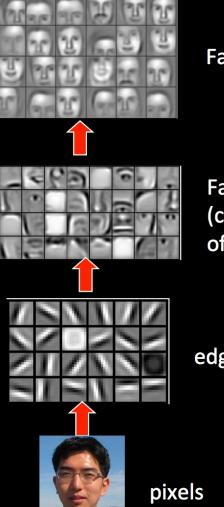
- Translation invariance (data-efficient to learn, less likely to overfit)
- Hierarchy



Hierarchically composed feature representations



Hierarchy of feature representations

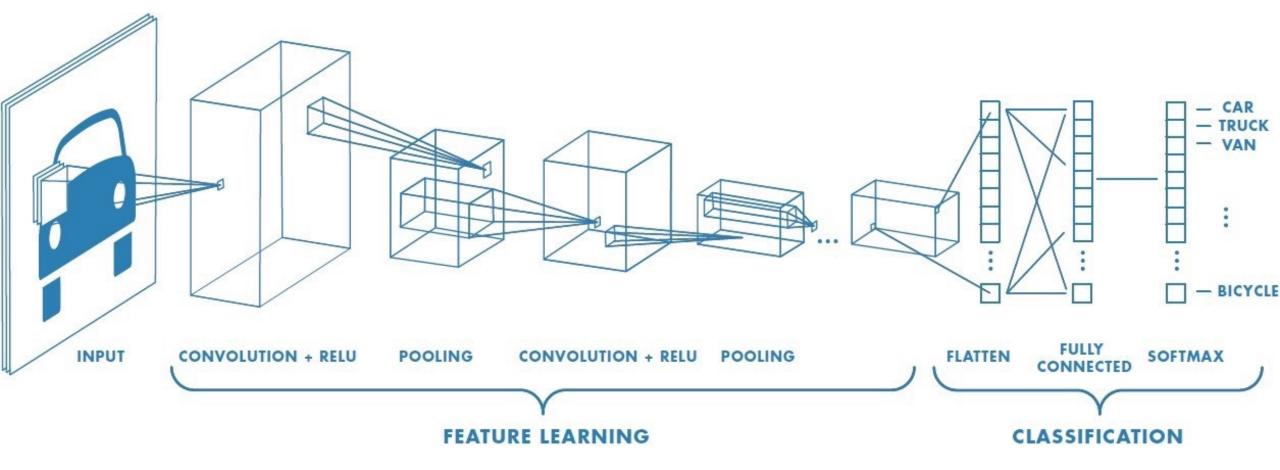


Face detectors

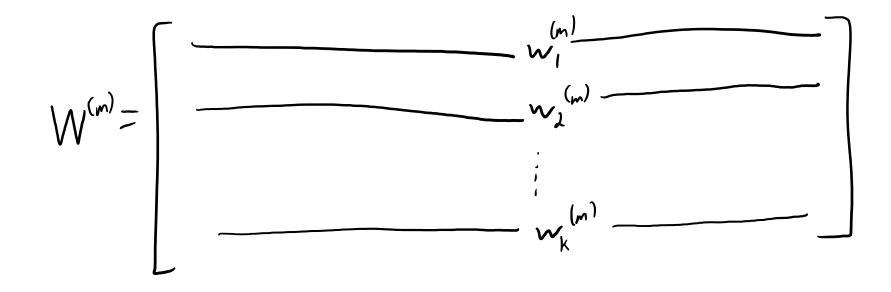
Face parts (combination of edges)

edges

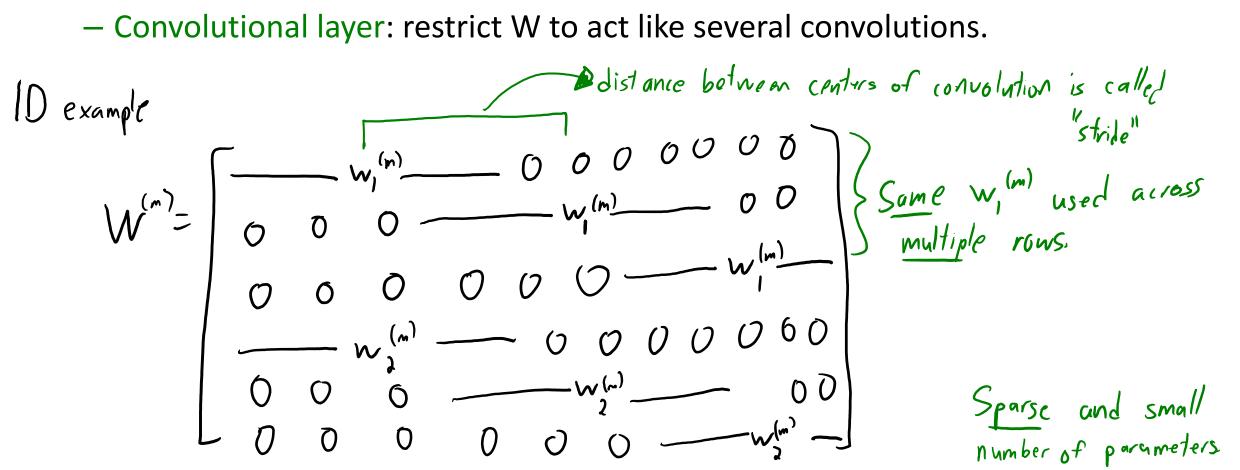
Lee et al, 2009.



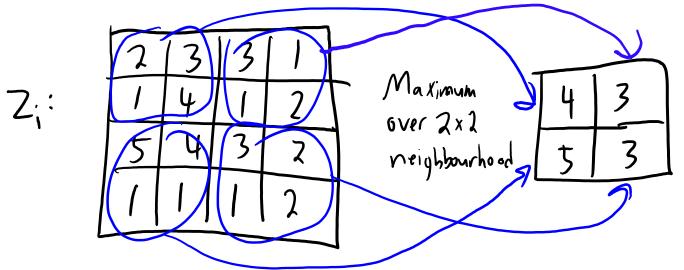
- Convolutional Neural Networks classically have 3 layer "types":
 - Fully connected layer: usual neural network layer with unrestricted W.



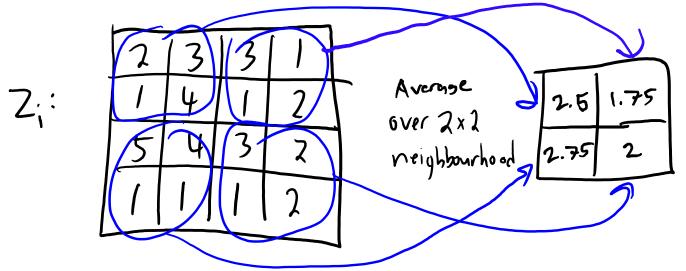
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 - Convolutional layer: restrict W to act like several convolutions.

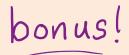


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 - Fully connected layer: usual neural network layer with unrestricted W.
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 - Pooling layer: combine results of convolutions.
 - Can add some invariance or just make the number of parameters smaller.
 - Often 'max pooling':



- Convolutional Neural Networks classically have 3 layer "types":
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 - Pooling layer: combine results of convolutions.
 - Can add some invariance or just make the number of parameters smaller.
 - Often 'max pooling' or else 'average pooling':

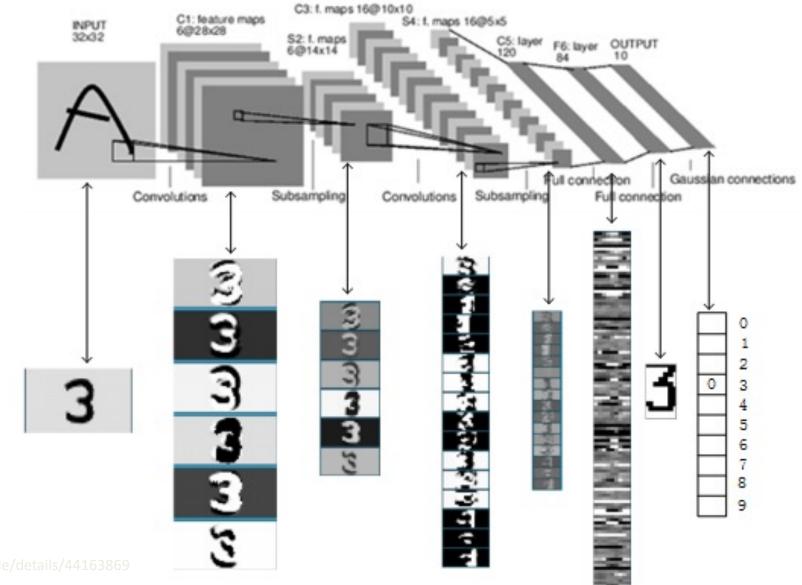




Max Pooling vs Average Pooling

- Both downsample the image
- Max pooling: "any of these options is present"
 - Much more common, especially in early layers
 - "There's an edge here, but I don't really care how thick it is"
- Average pooling: "all/most of these options are present"
 - If used, more often at the end of the network
 - "Most of the big patches look like a picture of a train"

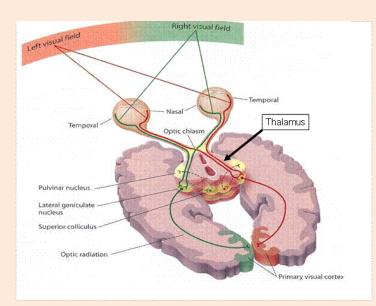
LeNet for Optical Character Recognition

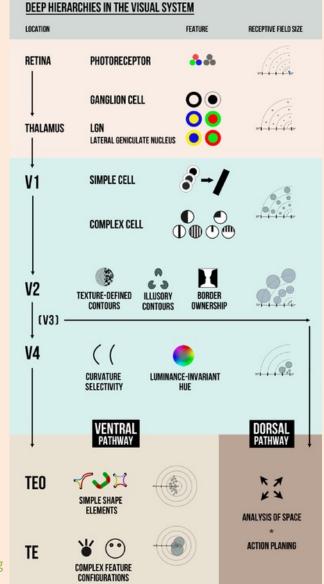


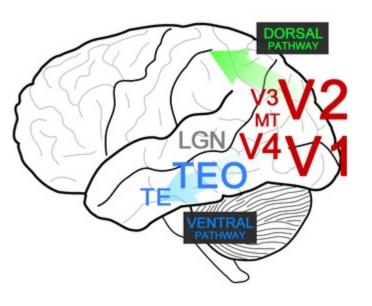
http://blog.csdn.net/strint/article/details/44163869



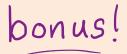
Deep Hierarchies in the Visual System



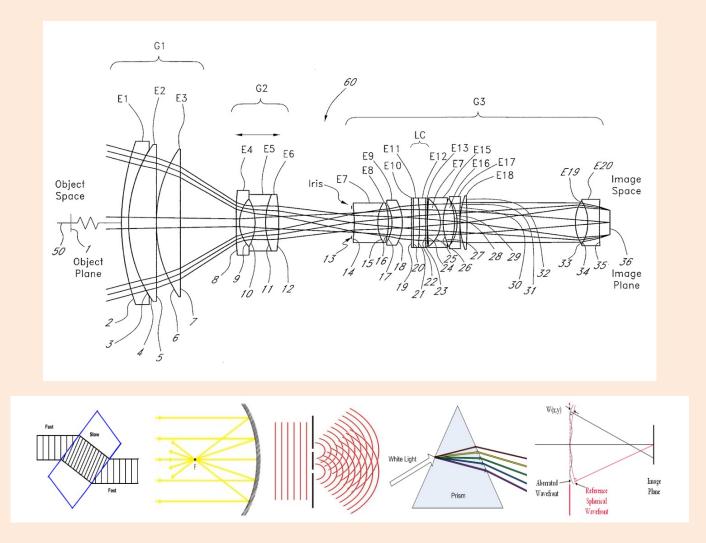




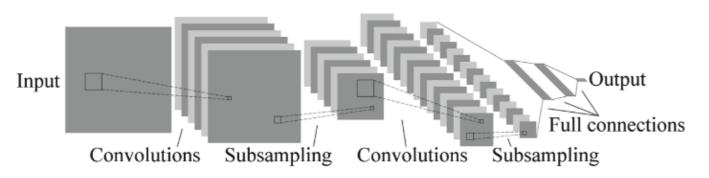
http://www.strokenetwork.org/newsletter/articles/vision.htm https://en.wikibooks.org/wiki/Sensory_Systems/Visual_Signal_Processing



Deep Hierarchies in Optics



• Classic convolutional neural network (LeNet):



- Visualizing the "activations" of the layers:
 - <u>http://scs.ryerson.ca/~aharley/vis/conv</u>
 - https://youtu.be/AgkflQ4IGaM



Next

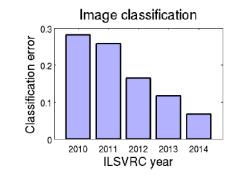
• A <u>very</u> small selection of key advances, things you should know, and tricks of the trade

Recent Lectures: Deep Learning

• We've been discussing neural network / deep learning models:

$$\gamma_{i} = \sqrt{h(W^{(m)}h(W^{(m-1)}h(----W^{(2)}h(W^{(1)}x_{i}))))}$$

- We discussed unprecedented vision/speech performance.
- We discussed methods to make SGD work better:
 - Parameter initialization and data transformations.
 - Setting the step size(s) in stochastic gradient and using momentum.
 - Alternative non-linear functions like ReLU.



max {0, zic}

"Residual" Networks (ResNets)

• Impactful recent idea is residual networks (ResNets):

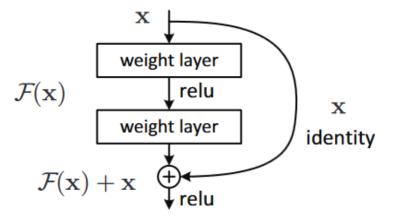


Figure 2. Residual learning: a building block.

- You can take previous (non-transformed) layer as input to current layer.
 - Also called "skip connections" or "highway networks".
- Non-linear part of the network only needs to model residuals.
 - Non-linear parts are just "pushing up or down" a linear model in various places.
- This was a key idea behind first methods that used 100+ layers.
 - Evidence that biological networks have skip connections like this.

DenseNet

- More recent variation is "DenseNets":
 - Each layer can see all the values from many previous layers.
 - Gets rid of vanishing gradients.
 - May get same performance with fewer parameters/layers.

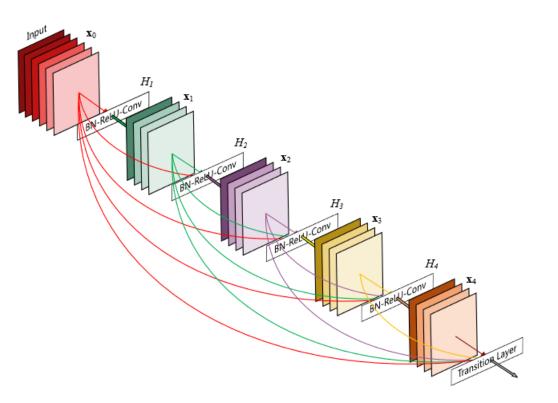


Figure 1: A 5-layer dense block with a growth rate of k = 4. Each layer takes all preceding feature-maps as input.

Deep Learning and the Fundamental Trade-Off

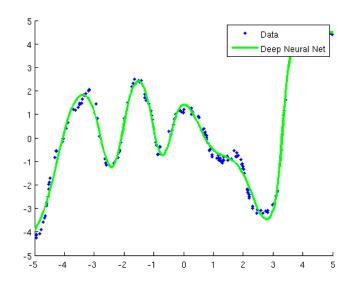
- Neural networks are subject to the fundamental trade-off:
 - With increasing depth, training error of global optima decreases.
 - With increasing depth, training error may poorly approximate test error.
- We want deep networks to model highly non-linear data.
 - But increasing the depth can lead to overfitting.
- How could GoogLeNet use 22 layers?
 - Many forms of regularization and keeping model complexity under control.
 - Unlike linear models, typically use multiple types of regularization.

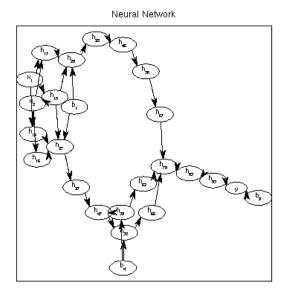
Standard Regularization

• Traditionally, we've added our usual L2-regularizers:

$$f(v_{1}W^{(3)},W^{(2)},W^{(1)}) = \frac{1}{2} \sum_{i=1}^{n} \left(\sqrt{h(W^{(3)}h(W^{(2)}h(W^{(2)}x_{i})))} - y_{i} \right)^{2} + \frac{1}{2} \frac{1$$

- L2-regularization often called "weight decay" in this context.
 - Could also use L1-regularization: gives sparse network.





Standard Regularization

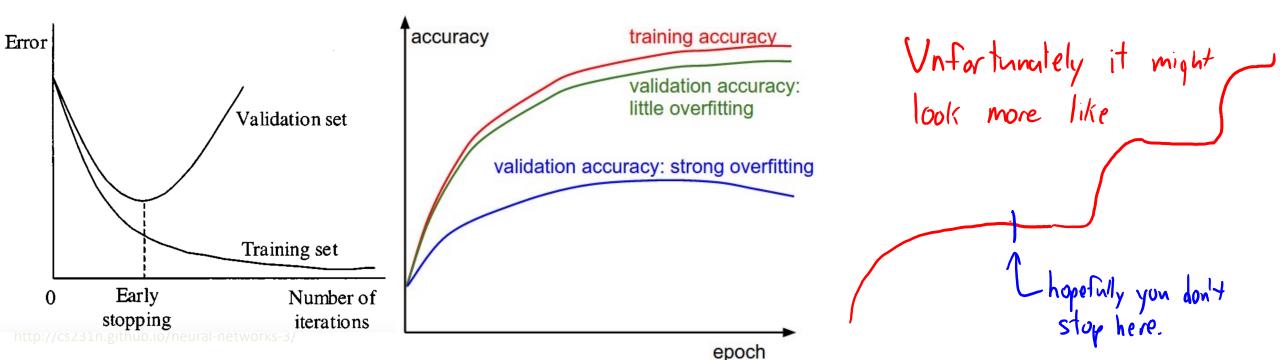
• Traditionally, we've added our usual L2-regularizers:

$$f(v_{1}W^{(3)}W^{(2)}W^{(1)}) = \frac{1}{2} \sum_{i=1}^{n} (v^{7}h(W^{(3)}h(W^{(2)}h(W^{(1)}x_{i}))) - y_{i})^{2} + \frac{1}{2} ||v||^{2} + \frac{1}{2} ||W^{(3)}||_{F}^{2} + \frac{1}{2} ||W^{(2)}||_{F}^{2} + \frac{1}{2} ||W^{(2)}||_{F}^{$$

- L2-regularization often called "weight decay" in this context.
 - Adds λ W to gradient, so (S)GD "decays" the weights 'W' at each step
 - Could also use L1-regularization: gives sparse network.
- Hyper-parameter optimization gets expensive:
 - Try to optimize validation error in terms of λ_1 , λ_2 , λ_3 , λ_4 .
 - In addition to step-size, number of layers, size of layers, initialization.
- Recent result:
 - Adding a regularizer in this way can create bad local optima.

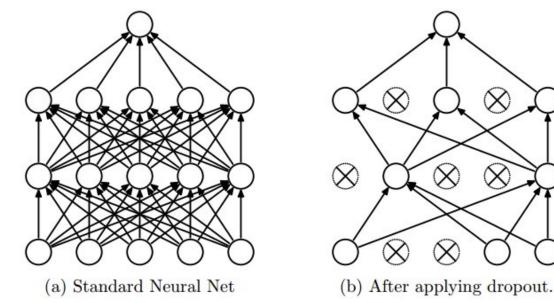
Early Stopping

- Another common type of regularization is "early stopping":
 - Monitor the validation error as we run stochastic gradient.
 - Stop the algorithm if validation error starts increasing.



Dropout

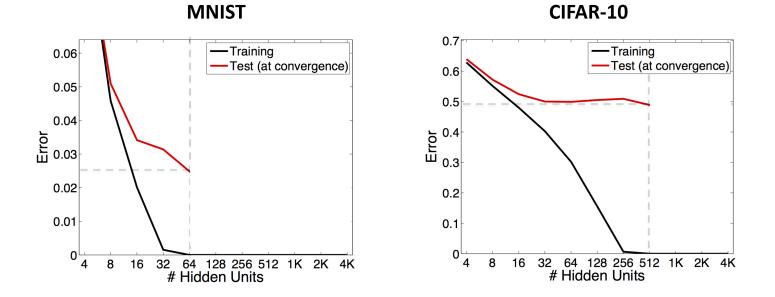
- **Dropout** is a more recent form of explicit regularization:
 - On each iteration, randomly set some x_i and z_i to zero (often use 50%).



- Adds invariance to missing inputs or latent factors
 - Encourages distributed representation rather than relying on specific z_i.
- Can be interpreted as an ensemble over networks with different parts missing.
- After a lot of early success, dropout is already kind of going out of fashion.

"Hidden" Regularization in Neural Networks

• Fitting single-layer neural network with SGD and no regularization:

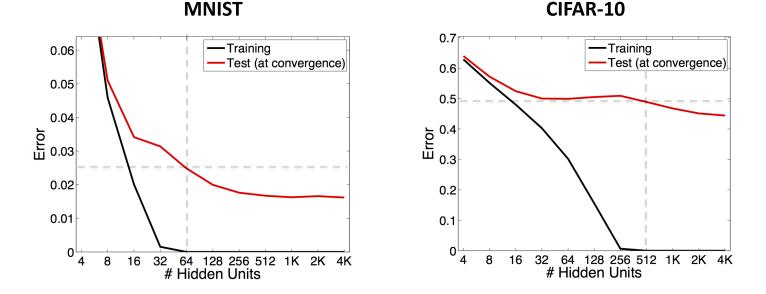


- Training goes to 0 with enough units: we're finding a global min.
- What should happen to training and test error for larger #hidden?

https://www.neyshabur.net/papers/inductive_bias_poster.pdf

"Hidden" Regularization in Neural Networks

• Fitting single-layer neural network with SGD and no regularization:



- Test error continues to go down!?! Where is fundamental trade-off??
- There exist global mins with large #hidden units have test error = 1.
 - But among the global minima, SGD is somehow converging to "good" ones.



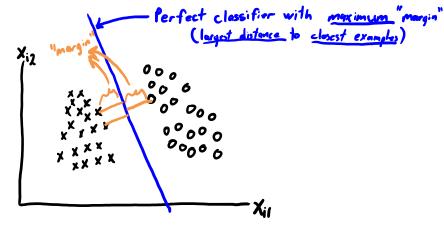
Implicit Regularization of SGD

- There is growing evidence that using SGD regularizes parameters.
 We call this the "implicit regularization" of the optimization algorithm.
- Beyond empirical evidence, we know this happens in simpler cases.
- Example of implicit regularization:
 - Consider a least squares problem where there exists a 'w' where X w = y.
 - Residuals are all zero, we fit the data exactly.
 - You run [stochastic] gradient descent starting from w=0.
 - Converges to solution X w = y that has the minimum L2-norm.
 - So using SGD is equivalent to L2-regularization here, but regularization is "implicit".



Implicit Regularization of SGD

- Example of implicit regularization:
 - Consider a logistic regression problem where data is linearly separable.
 - We can fit the data exactly.
 - You run gradient descent from any starting point.
 - Converges to max-margin solution of the problem.
 - So using gradient descent is equivalent to encouraging large margin.



• Similar result known for boosting.

(pause)

Deep Learning "Tricks of the Trade"

- We've discussed heuristics to make deep learning work:
 - Parameter initialization and data transformations.
 - Setting the step size(s) in stochastic gradient and using momentum.
 - RestNets and alternative non-linear functions like ReLU.
 - Different forms of regularization:
 - L2-regularization, early stopping, dropout, implicit regularization from SGD.
- These are often still not enough to get deep models working.
- Deep computer vision models are all convolutional neural networks:
 - The W^(m) are very sparse and have repeated parameters ("tied weights").
 - Drastically reduces number of parameters (speeds training, reduces overfitting).

Summary

- ResNets include untransformed previous layers.
 - Network focuses non-linearity on residual, allows huge number of layers.
- Regularization is crucial to neural net performance:
 - L2-regularization, early stopping, dropout, implicit regularization of SGD.
- Convolutional neural networks:
 - Restrict W^(m) matrices to represent sets of convolutions.
 - Often combined with max (pooling).

Next time: modern convolutional neural networks and applications.
 – Image segmentation, depth estimation, image colorization, artistic style.